

What do you know / what are you trying to find???

1. You know 'x' - find 'y'

Sub in 'x'  
 Solve for 'y'

2. You know 'y' - find 'x'

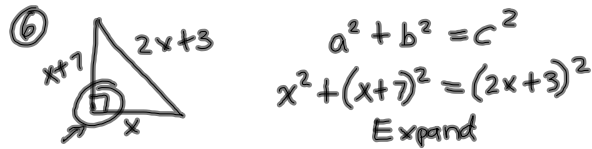
Sub in 'y'  
 → Solve for 'x'

- ① Standard form → quadratic formula  
 → factor
- ② Factored form → find zeros from factors  $(x-3)(x+4)$   
 - what makes each factor = 0     $\downarrow$   $x=3$      $\downarrow$   $x=-4$
- ③ Vertex form → solve directly  
 $0 = 2x^2 - 4$   
 $0 = 2(x-4)^2 - 16$

3. You need to find the vertex

- ① Standard → complete the square
- ② Factored → use zeros to find 'x' value of vertex,  $\frac{r+s}{2}$   
 sub in to equation to find 'y'
- ③ Vertex form → vertex (h,k)  
 $y = 2(x-4)^2 - 16$   
 $\quad \quad \quad \underset{h}{4} \quad \underset{k}{-16}$

6 9 11 21 ~~12~~ 17 18



$$a^2 + b^2 = c^2$$

$$x^2 + (x+7)^2 = (2x+3)^2$$

Expand

factor

$$2x^2 - 2x - 40 = 0$$

q. form

$$2(x^2 - x - 20) = 0$$

$$2(x-5)(x+4) = 0$$

M: -20  
A: -1  
N: -5, 4

$x=5$   $x=-4$  inadmissible

$$x+7=12$$

$$2x+3=13$$

⑨ A = multiply 2 things = QUADRATIC

$$A = \frac{bh}{2}$$

$$2 \times 20 = \frac{b(b+4)}{2}$$

$$40 = b^2 + 4b$$

$$0 = b^2 + 4b - 40$$

factor → q form

$b = 4.63 \text{ cm}$   
 $b = 46 \text{ mm}$

⑩  $p = 23$   
 $p = 2l + 2w$   
 $23 = 2l + 2w$   
 $\frac{23-2w}{2} = \frac{2l}{2}$   
 $\frac{23}{2} - w = l$

$A = 33$  \* Area = quadrate  
 $A = lw$   
 $33 = lw$   
 $33 = (\frac{23}{2} - w)w$   
 $33 = \frac{23w}{2} - w^2$   
 $w^2 - \frac{23}{2}w + 33 = 0$   
Solve → quad form.

⑪ a) Revenue = Price x # Sold  
 $= (10 - 0.5x)(30 + 2x)$

b)  $R = 150$   
 $150 = (10 - 0.5x)(30 + 2x)$   
 $150 = 300 + 20x - 15x - x^2$   
 $0 = -x^2 + 5x + 150$   
 $0 = -(x^2 - 5x - 150)$   
 $0 = -(x-15)(x+10)$   
 $x=15$   $x=-10$

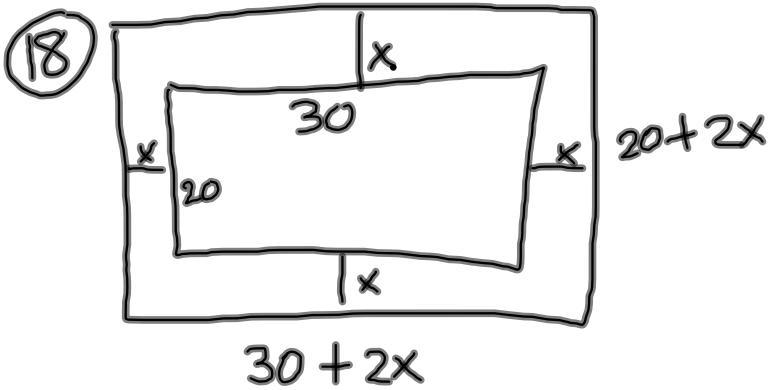
M: 150  
A: -5  
N: -15, 10

Price  
 $10 - 0.5x$   
 $= 10 - (0.5)(15)$   
 $= 2.50$   
OR  
 $10 - 0.5(-10)$   
 $= 10 + 5$   
 $= 15$

c) vertex complete the square  $x = \frac{15 + (-10)}{2}$

d)  $0 = 300 + 15x - x^2$  → factor  
→ quad form





$$A = l \cdot w$$

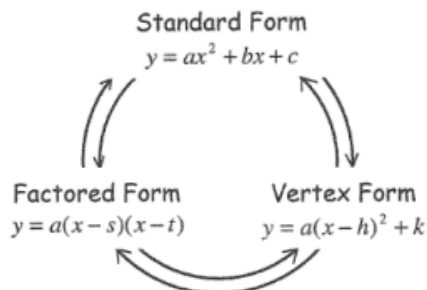
$$1064 = (20 + 2x)(30 + 2x)$$

Expand

Set = 0

Solve  $\rightarrow$  factor  
 $\rightarrow$  q. form.

Everything I Need to Know about Quadratics...But Was Afraid to Ask!



If you want...	And you have...	Then do this
<b>Vertex Form</b> $y = a(x-h)^2 + k$	<b>Standard Form</b> $y = ax^2 + bx + c$	> complete the square or > solve for zeros and use to calculate vertex > "a" will be the same
	<b>Factored Form</b> $y = a(x-s)(x-t)$	> expand to standard form then convert to vertex form or > solve for zeros and use to calculate vertex > "a" will be the same
<b>Standard Form</b> $y = ax^2 + bx + c$	<b>Vertex Form</b> $y = a(x-h)^2 + k$	> expand
	<b>Factored Form</b> $y = a(x-s)(x-t)$	> expand
<b>Factored Form</b> $y = a(x-s)(x-t)$	<b>Vertex Form</b> $y = a(x-h)^2 + k$	> convert to standard form, then convert to factored form or > solve for zeros and substitute into factored form > "a" will be the same
	<b>Standard Form</b> $y = ax^2 + bx + c$	> factor, if possible or > use quadratic formula to find zeros and substitute into factored form or > may not have factored form if there are no real roots
<b>to graph</b>	<b>Vertex Form</b> $y = a(x-h)^2 + k$	> read vertex/transformations directly from equation ✓ h is horizontal ✓ k is vertical ✓ a is reflection and stretch/compression for improved accuracy, consider finding y-intercept or applying step pattern.
	<b>Standard Form</b> $y = ax^2 + bx + c$	> solve for x-intercepts and y-intercept or > solve for vertex and y-intercept
	<b>Factored Form</b> $y = a(x-s)(x-t)$	> read zeros from equation, solve for y-intercept or vertex

If you want...	And you have...	Then do this
y-intercept	Vertex Form $y = a(x-h)^2 + k$	➤ set $x = 0$ and solve for $y$
	Standard Form $y = ax^2 + bx + c$	➤ set $x = 0$ and solve for $y$ or ➤ $c$
	Factored Form $y = a(x-s)(x-t)$	➤ set $x = 0$ and solve for $y$
vertex, max/min, optimal value	Vertex Form $y = a(x-h)^2 + k$	➤ read the vertex right from the equation: $(h,k)$
	Standard Form $y = ax^2 + bx + c$	➤ convert to vertex form or ➤ determine the zeros and use $\frac{s+t}{2}$ to get $x$ -coordinate of vertex (axis of symmetry) ➤ substitute this $x$ to get the $y$ -coordinate or ➤ use $x = -\frac{b}{2a}$ to get $x$ -coordinate of vertex ➤ Substitute this $x$ to get the $y$ -coordinate
	Factored Form $y = a(x-s)(x-t)$	➤ use the zeros and $\frac{s+t}{2}$ to get $x$ -coordinate of vertex (axis of symmetry) ➤ substitute this $x$ to get the $y$ -coordinate or ➤ convert to standard form then complete the square
x-intercepts, zeros, roots	Vertex Form $y = a(x-h)^2 + k$	➤ convert to standard form then factor or use quadratic formula or ➤ set $y = 0$ then solve for $x$ using inverse operations
	Standard Form $y = ax^2 + bx + c$	➤ factor if possible or ➤ use quadratic formula or ➤ may not have real roots
	Factored Form $y = a(x-s)(x-t)$	➤ read the zeros right from the equation: $s$ & $t$
the number of zeros	Vertex Form $y = a(x-h)^2 + k$	➤ analyze location of vertex and opening direction, draw conclusions
	Standard Form $y = ax^2 + bx + c$	➤ use discriminant: $D < 0$ , $D = 0$ , $D > 0$
	Factored Form $y = a(x-s)(x-t)$	➤ zeros are given in this form