

5, b, a

"Amount over Cost Price"

$$\begin{aligned}
 \textcircled{5} \text{ Revenue} &= \text{Profit} + x \text{ \# Sold} \\
 &= (800 + 20x)(60 - x) \\
 &= 48000 - 800x + 1200x - 20x^2 \\
 &= -20x^2 + 400x + 48000 \\
 &= -20(x^2 - 20x + 100 - 100) + 48000 \\
 &= -20(x - 10)^2 + 2000 + 48000 \\
 &= -20(x - 10)^2 + 50000
 \end{aligned}$$

$x = 10$

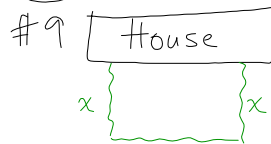
Max Revenue (we don't need)

∴ Amount over Cost Price
 $= 800 + 20x$
 $= 800 + 20(10)$
 $= 81000$

$$\begin{aligned}
 \textcircled{6} \text{ Profit} &= (30 - 1.50x)(60 + 10x) \quad \text{\# of people} \\
 &= 1800 + 300x - 90x - 15x^2 \\
 &= -15x^2 + 210x + 1800 \\
 &= -15(x^2 - 14x + 49 - 49) + 1800 \\
 &= -15(x - 7)^2 + 735 + 1800 \\
 &= -15(x - 7)^2 + 2535
 \end{aligned}$$

$x = 7$

\# of people = $60 + 10x$
 $= 60 + 10(7)$
 $= 130$



$A = l \cdot w$
 $= x(24 - 2x)$

$$\begin{aligned}
 &= 24x - 2x^2 \\
 &= -2x^2 + 24x \\
 &= -2(x^2 - 12x + 36 - 36) \\
 &= -2(x - 6)^2 + 72
 \end{aligned}$$

$P = 2x + y$
 $24 = 2x + y$
 $24 - 2x = y$

$x = 6m$
 $y = 24 - 2x$
 $y = 12m$

∴ 6m by 12m

∴ most efficient = vertex

$$\begin{aligned}
 C(v) &= 0.0029v^2 - 0.48v + 142 \\
 &= 0.0029(v^2 - \frac{4800}{29}v) + 142 \\
 &= 0.0029(v^2 - \frac{4800}{29}v + \frac{5760000}{841} - \frac{5760000}{841}) + 142
 \end{aligned}$$

$\frac{4800}{29} \times \frac{1}{2}$

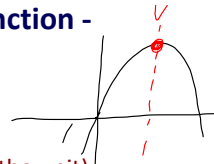
$(\frac{2400}{29})^2$

$\frac{5760000}{841}$

1.3B Maximum or Minimum of a Quadratic Function - Partial Factoring

Recall that to find the vertex we can:

- Complete the square (time consuming)
- Factor -> Vertex falls halfway between the zeros (later in the unit)



And now for something sort of brand new...

Finding the Vertex by Partial Factoring

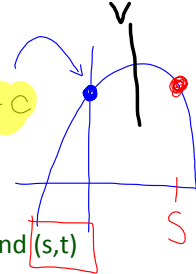
$$y = ax(x-s) + t$$

$$y = ax^2 + bx + c$$

$$x=0, y=t \rightarrow x=s, y=t$$

- determines 2 points that are the same height (0,t) and (s,t)

$$y=nt$$



- these points can then be used to determine the vertex

$$y = ax^2 + bx + c$$

Here is the technique:

- * Remove "ax" from first 2 terms
Then, if $x = 0, y = t$
if $x = s, y = t$

★ (0,t) and (s,t) are points on the graph at a height of 't'

★ When you have these 2 points at the same height, you can use symmetry to find the vertex.

These points are NOT the Zeros!!!

Consider:

$$y = 3x^2 - 24x + 3$$

What is the y-intercept?

$$(0, 3)$$

Partially Factored:

$$y = 3x(x-8) + 3$$

$$x=0, y=3 \quad x=8, y=3$$

What is the y-intercept?

$$(0, 3)$$

What other value of x gives this y-value?

$$(8, 3)$$

What is the axis of symmetry?

$$x = \frac{0+8}{2}$$

$$x = 4$$

What is the vertex?

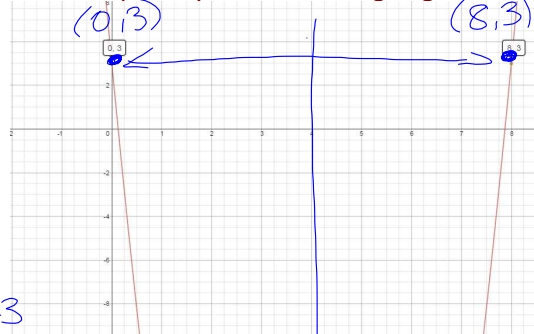
$$y = 3x^2 - 24x + 3$$

$$y = 3(4)^2 - 24(4) + 3$$

$$y = -45$$

∴ Vertex (4, -45)

Graphically this is what is going on:



Ex. 1 Use partial factoring to determine the vertex.

a) $y = 2x^2 + 10x + 1$

$= 2x(x+5) + 1$

$x = 0$

$y = 1$

$(0, 1)$

Vertex

$x = \frac{0 + (-5)}{2}$

$x = -\frac{5}{2}$

$x = -5$

$y = 1$

$(-5, 1)$

$y = 2x^2 + 10x + 1$

$= 2\left(-\frac{5}{2}\right)^2 + 10\left(-\frac{5}{2}\right) + 1$

$= 2\left(\frac{25}{4}\right) - 25 + 1$

$= \frac{25}{2} - \frac{48}{2}$

$y = -\frac{23}{2}$

$-24 \rightarrow -\frac{48}{2}$

$V\left(-\frac{5}{2}, -\frac{23}{2}\right)$

b) $y = -2x^2 + 8x - 13$

$V(2, -5)$

c) $y = -x^2 + 5x - 3$ $V\left(\frac{5}{2}, \frac{13}{4}\right)$

d) $y = 5x^2 - 2x + 1$ $\left(\frac{1}{5}, \frac{4}{5}\right)$

Homework

p. 31 #3

Handout

Word

Pr: 1a, 3b, 4, 5, 6, 8

#1, 2

enough to be partial factoring experts (v)