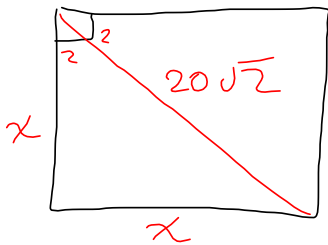


17, 20, 12

(12)



$$a^2 + b^2 = c^2$$

$$x^2 + x^2 = (20\sqrt{2})^2$$

$$x = 20$$

of sq = 10

$$10 \times 10$$

$$= 100$$

(17)

$$\begin{aligned} a) & \sqrt[3]{54} \\ &= \sqrt[3]{27 \cdot 2} \\ &= 3 \sqrt[3]{2} \end{aligned}$$

$$1^3 = 1$$

$$2^3 = 8$$

$$3^3 = 27$$

$$4^3 = 64$$

1.5A Factoring

$$3(x+2) \xrightleftharpoons[\text{Factor}]{\text{Expand/Multiply}} 3x+6$$

To factor is to write an algebraic expression as a **product** of two or more other algebraic expressions .

Why factor? To arrive at equivalent expressions which are presented in simpler terms which allows us to:

- Solve equations
- Graph relations

In grade 10 you learned how to:

- Common Factor
- Factor by Grouping
- Factor Simple Trinomials
- Factor Complex Trinomials
- Factor a Difference of Squares
- Factor a Perfect Square Trinomial

Common Factoring



Always your first and last step.



WHEN?

2 or more terms

HOW?

- Take out the greatest common factor.
- Divide the expression by the GCF to find the other factor.

a) $2mn - 4mnt$
 $= 2mn(1 - 2t)$

b) $6t^5 - 9t^2$
 $= 3t^2(2t^3 - 3)$

c) $3x^4 - 6x^3 + 9x$
 $= 3x(x^3 - 2x^2 + 3)$

d) $4x(a-b) - 3(a-b)$
 $= (a-b)(4x - 3)$

Factor by Grouping

WHEN?

An even # of terms: 4, 6, 8, etc...

HOW?

- Group terms to form pairs.
- Factor the pairs by finding common factors.
- Factor out the shared common binomial factor.

$$\begin{aligned} \text{a) } & 3x(m-5) + 2(5-m) \\ & = 3x(\underline{m-5}) - 2(\underline{m-5}) \\ & = (m-5)(3x-2) \end{aligned}$$



The terms $m-5$ and $5-m$ are opposites. This means that one divided by the other is -1 .

$$\begin{aligned} \text{b) } & x(y-2) - 4(2-y) \\ & = x(y-2) + 4(y-2) \\ & = (y-2)(x+4) \end{aligned}$$

$$\begin{aligned} \text{c) } & \underline{mx} + \underline{2y} + \underline{my} + \underline{2x} \\ & = \underline{mx+my} + \underline{2y+2x} \\ & = m(x+y) + 2(x+y) \\ & = (x+y)(m+2) \end{aligned}$$

$$\begin{aligned} \text{d) } & \underline{22vx - 6vy} + \underline{11wx - 3wy} \\ & = 2v(11x-3y) + w(11x-3y) \\ & = (11x-3y)(2v+w) \end{aligned}$$

$$\begin{aligned} \text{e) } & \underline{y^2+1} - \underline{y^3-y} \\ & = \underline{(y^2+1)} - y(\underline{y^2+1}) \\ & = (y^2+1)(1-y) \end{aligned}$$

$$\begin{aligned} \text{f) } & \underline{16x^5 + 8x^4} - \underline{6x^3 - 3x^2} + \underline{4x + 2} \\ & = 8x^4(\underline{2x+1}) - 3x^2(\underline{2x+1}) + 2(\underline{2x+1}) \\ & = (2x+1)(8x^4 - 3x^2 + 2) \end{aligned}$$

Simple Trinomials

WHEN?

3 terms
 $ax^2 + bx + c$ where $a = 1$

HOW?

$$(x + n_1)(x + n_2)$$

$$\begin{aligned} M &= ac \\ A &= b \\ N &= n_1, n_2 \end{aligned}$$

a) $x^2 - 9x + 14$
 $= (x - 7)(x - 2)$

$$\begin{aligned} M &: 14 \\ A &: -9 \\ N &: -2, -7 \end{aligned}$$

b) $5x^2 + 15x - 140$
 $= 5(x^2 + 3x - 28)$
 $= 5(x + 7)(x - 4)$

c) $a^2 + 8ab + 15b^2$
 $(a + 5b)(a + 3b)$

$$\begin{aligned} M &: 15 \\ A &: 8 \\ N &: 5, 3 \end{aligned}$$

d) $x^4 + 2x^2b - 24b^2$
 $= (x^2 + 6b)(x^2 - 4b)$

$$\begin{aligned} M &: -24 \\ A &: 2 \\ N &: 6, -4 \end{aligned}$$

Difference of Squares

WHEN?

2 terms

2 perfect squares separated
by a subtraction: $a^2 - b^2$

a) $49x^2 - 16y^2$

$$= (7x - 4y)(7x + 4y)$$

c) $a^2 - \frac{1}{9}$

$$= \left(a - \frac{1}{3}\right)\left(a + \frac{1}{3}\right)$$

$$\sqrt{\frac{1}{9}} = \frac{1}{3}$$

e) $(3x-2)^2 - (5x+1)^2$

$$= [(3x-2) - (5x+1)][(3x-2) + (5x+1)]$$

$$= (3x-2-5x-1)(3x-2+5x+1)$$

$$= (-2x-3)(8x-1)$$

$$= -(2x+3)(8x-1)$$

HOW?

$$a^2 - b^2 = (a - b)(a + b)$$

conjugates

b) $3x^2 - 12$

$$= 3(x^2 - 4)$$
$$= 3(x-2)(x+2)$$

d) $81 - m^{12}$

$$= (9 - m^6)(9 + m^6)$$
$$= (3 - m^3)(3 + m^3)(9 + m^6)$$

$$m^6 \cdot m^6$$

$$\sqrt{(3x-2)^2}$$
$$= (3x-2)$$

Complex Trinomials

WHEN?

3 terms
 $ax^2 + bx + c$ where $a \neq 1$

HOW?

$$(a_1x + f_1)(a_2x + f_2)$$

$$\begin{aligned} M &= ac \\ A &= b \\ N &= n_1, n_2 \end{aligned}$$

1. Use a, n_1 and n_2 to find the factors.

2. Reduce.

$$\frac{a}{n_1}, \frac{a}{n_2}$$

$$\frac{a_1}{f_1}, \frac{a_2}{f_2}$$

OR

Decompose the middle term using n_1, n_2 and factor by grouping.

a) $10x^2 - 11x - 6$
 $= (2x - 3)(5x + 2)$

$M: -60$
 $A: -11$
 $N: -15, 4$

$$\begin{array}{r} \frac{10x}{-15} \quad \frac{10x}{4} \\ = \frac{2x}{-3} \quad \frac{5x}{2} \end{array}$$

b) $14x^2 + 31xy - 10y^2$
 $= (2x + 5y)(7x - 2y)$

$M: -140$
 $A: 31$
 $N: 35, -4$

$$\begin{array}{r} \frac{14x}{35y} \\ = \frac{2x}{5y} \end{array} \quad \begin{array}{r} \frac{14x}{-4y} \\ = \frac{7x}{-2y} \end{array}$$

c) $18a^2b + 3ab - 6b$
 $= 3b(6a^2 + a - 2)$
 $= 3b(3a + 2)(2a - 1)$

$M: -12$
 $A: 1$
 $N: 4, -3$

$$\begin{array}{r} \frac{4}{6a} \quad \frac{-3}{6a} \\ = \frac{2}{3a} \quad \frac{-1}{2a} \end{array}$$

e) $2x^2 - 3x - 5$
 $= (2x - 5)(x + 1)$

$$\begin{array}{r} \frac{-5}{2x} \quad \frac{2}{2x} \\ = \frac{-1}{x} \end{array}$$

Perfect Square Trinomials

WHEN?

3 terms

$$ax^2 + bx + c$$

where **a** & **c** are perfect squares and **b** is twice the product of their square roots.

$$\hookrightarrow b = 2\sqrt{a}\sqrt{c}$$

HOW?

$$\text{OR} \\ (\sqrt{ax} \pm \sqrt{c})^2$$

same sign as b

a) $m^2 + 10m + 25$
 $= (m + 5)^2$

b) $2x^2 - 24x + 72$
 $= 2(x^2 - 12x + 36)$
 $= 2(x - 6)^2$

c) $16a^2 + 24a + 9$
 $= (4a + 3)^2$

d) $x^4 - 8x^2 + 16$

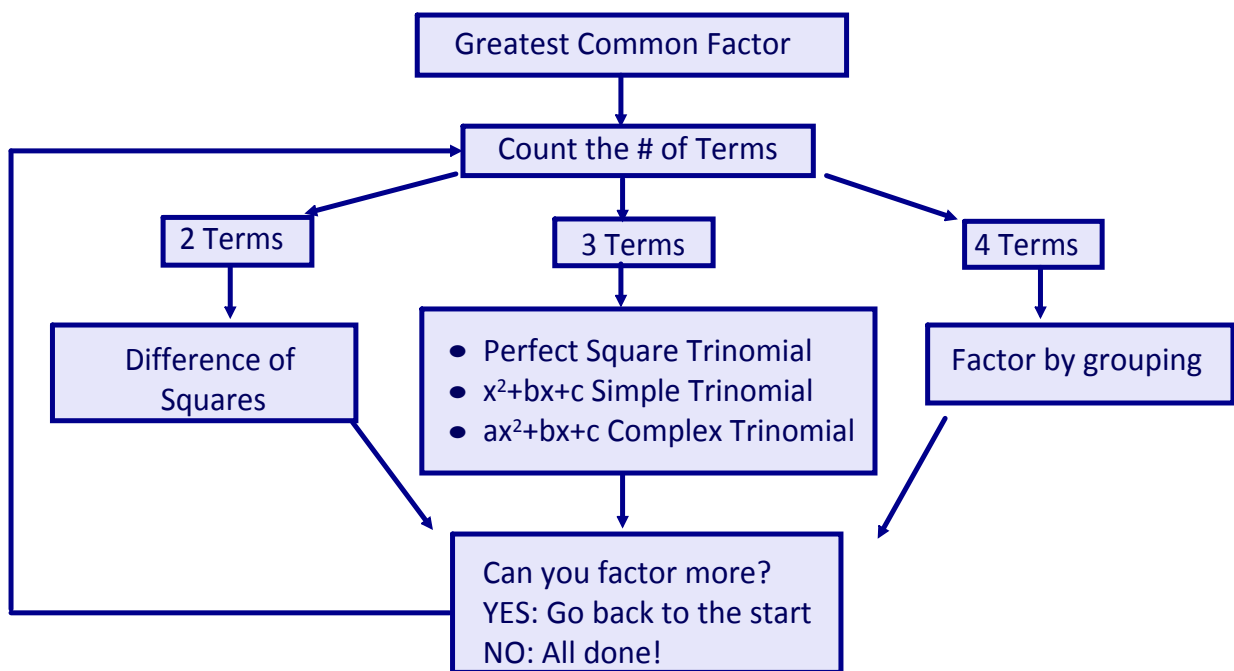
$$= (x^2 - 4)^2$$

$$= (x^2 - 4)(x^2 - 4)$$

$$= (x - 2)(x + 2)(x - 2)(x + 2)$$

$$= (x - 2)^2(x + 2)^2$$

Factoring Flowchart



Check you answer by
EXPANDING

HOMEWORK
Handout 1.6

$2x^2 + 9x + 10$

	$2x$	5
x	$2x^2$	$5x$
2	$4x$	10

$(x+2)(2x+5)$

20
 \wedge
 $1 \quad 20$
 $2 \quad 10$
 $4 \quad 5$