7.3 Minimum Perimeter for a Given Area

Investigation: page 61 in text.

Michael has 36 square stones to arrange as a rectangular patio. He will

then buy edging to go around the patio.

• Sketch a few of the different patios that can be created.



Which patio requires the least amount of edging?

Area	Length	Width Divide area by the length	Perimeter $P = 2 l + 2 w$
36	1	36 ÷1= 36	2(1) + 2(36) = 74
36	5	7.2	Don't use 5 as we can't have part of a stone.

Minimum perimeter



- \Rightarrow For rectangles with a <u>fixed</u> area, a square has the <u>minimum perimeter</u>.
 - Suppose each stone has a side length of 30 cm.
 What is the least amount of edging needed for the patio?

Ex. 1: For 75 patio stones, what are the dimensions that give the minimum perimeter?

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length	width	perimeter

If it is not possible to form a square, (sides are restricted to whole numbers) then the minimum perimeter occurs when the rectangle is closest to a square.

Ex. 2: What is the minimum perimeter of a rectangle having an area of:

a) 121 cm²

b) 90 cm²

Ex. 3: A patio is to be built on the side of a house using 24 congruent square stones. It will then be edged on 3 sides. Which arrangement requires the minimum edging?



THINK List pairs of numbers with product 24. Calculate perimeter using 3 sides only!

length	width	perimeter

HOMEWORK

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